

Twin Cities ANSYS[®] User Meeting

November 2011

Mesh Discretization Error





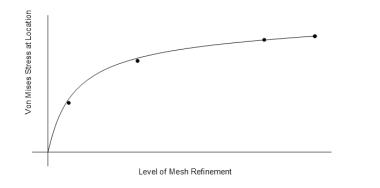
- 1. Mesh Discretization: The "One-sided" Error Source
- 2. Tet Pregidous
- 3. Case Study A: Shape-Functions Effect
 - With and without mid-side nodes
 - Stresses & Deflection
- 4. Case Study B: Mesh Convergence
 - Node vs. Element (Averaged vs Unaveraged)
 - PRERR (SEPC/SMXB)



- Often small compared to load/material property error/scatter
- Ownership of error lands on analyst
 - Often linked to "credibility" of whole analysis
- True Error analysis would likely show Mesh Discretization is minor issue
 - And yet... Scrutiny continues
 - And rules and criteria abound... (while other scatter goes unmentioned)
- "It can be *measured*? Well let's fixate on it!"



- A "one-sided" error source*
 - Predictions are usually *lower* than actual (not higher)
 - Excepting Singularities
 - Nagging feeling because of non-conservative nature
 - Stress is usually underpredicted*
 - Upper bound not determinable
 - Without employing knowledge of materials/loads/element shape functions discussed later



*Powergraphics results (classic) isn't so one-sided – discussed later

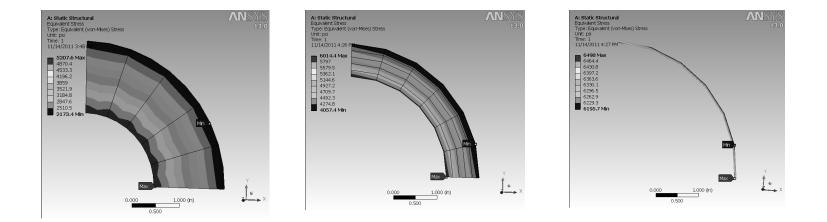


- Bias Against Tetrahedrons (Tet's)
 - Source of grievance?
 - Low order Tets (a.k.a "T4", a.k.a "non-midside noded Tet")
 - Too Stiff in bending / large error with 1 element through thickness
 - 1st Tet's (Berkely 1960's) were high order
 - You'd have to work at it to get ANSYS to create T4's (structural)
 - Tets (10 noded) are Less efficient per DOF
 - Longer solve times
 - Shorter meshing times
 - Added control allows refinement at location of interest
 - More efficient than Mapped meshing!
 - Less pleasing to the eye (esp. higher aspect ratios)
 - Stigmatism is receding over last decade

Case Study A

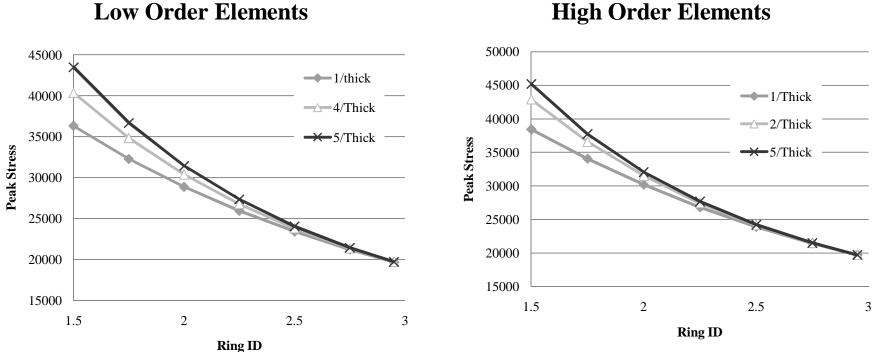


- Thick to thin rings with inner pressfit (radial expansion)
 - Stress gradient related to radius²
- Case Study A, Expansion of Thick/Thin Ring
 - Actually used 5° wedge





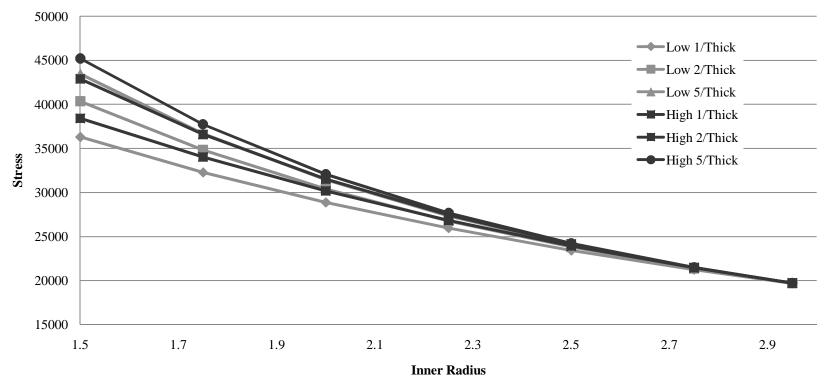
- Case Study A
 - Peak Stresses have similar convergence patterns/rate



High Order Elements



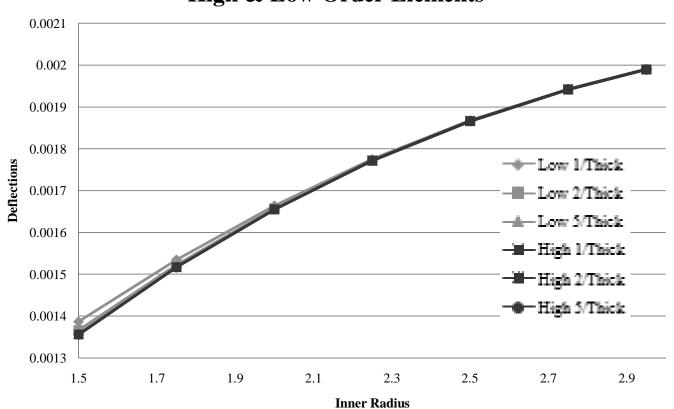
- Case Study A
 - Peak Stresses have similar convergence patterns/rate



High & Low Order Elements



- Case Study A
 - OD Deflections

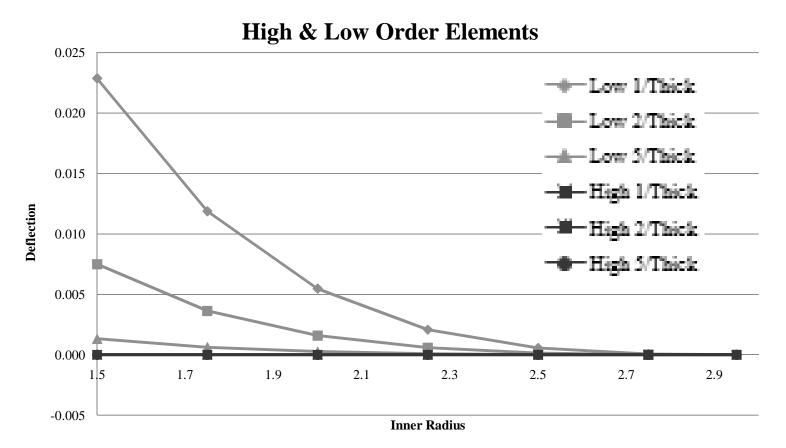


High & Low Order Elements

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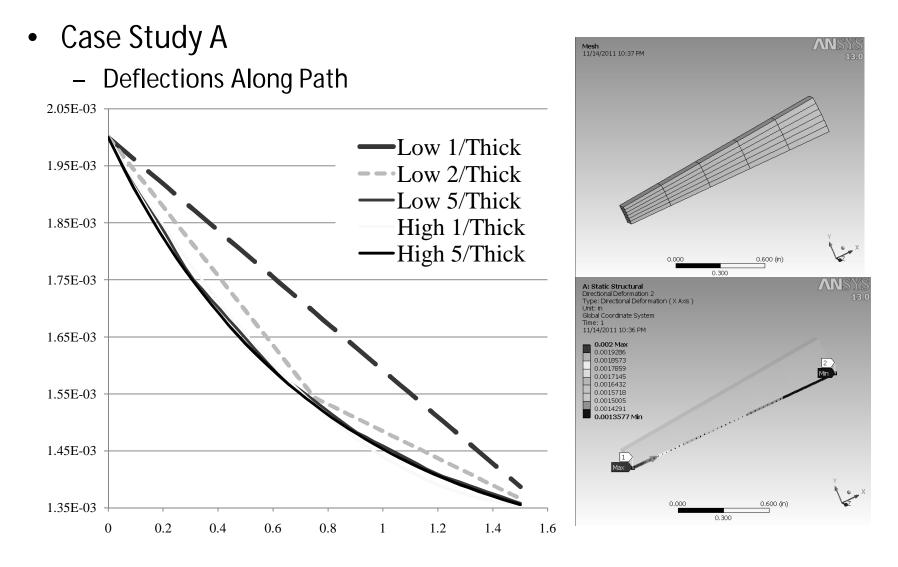


- Case Study A
 - OD Deflections



Case Study A





Case Study A

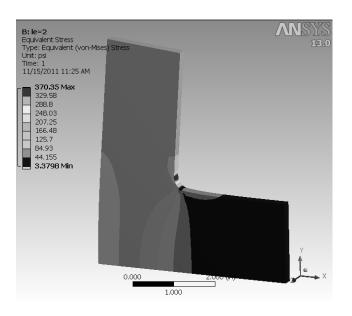


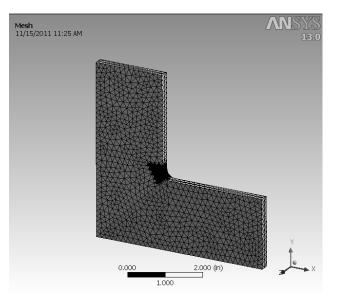
- Case Study A Conclusions
 - Element Stress Gradient
 - Linear for high or low order elements
 - Element Displacement Gradient
 - Linear for low order element
 - 2nd order polynomial for high order element
 - Thin Rings are well approximated with single element through the thickness
 - This extends to beams as well

Mesh Discretization Error



- Case Study B
 - Stress along path
 - Node vs. Element (Averaged vs Unaveraged)
 - PRERR (SEPC/SMXB)



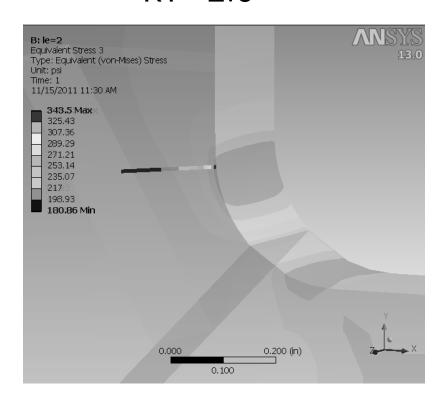


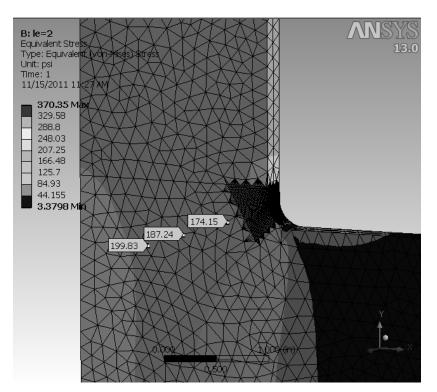
Case Study B



Stress along path

 Background stress of 180
 KT = 2.0

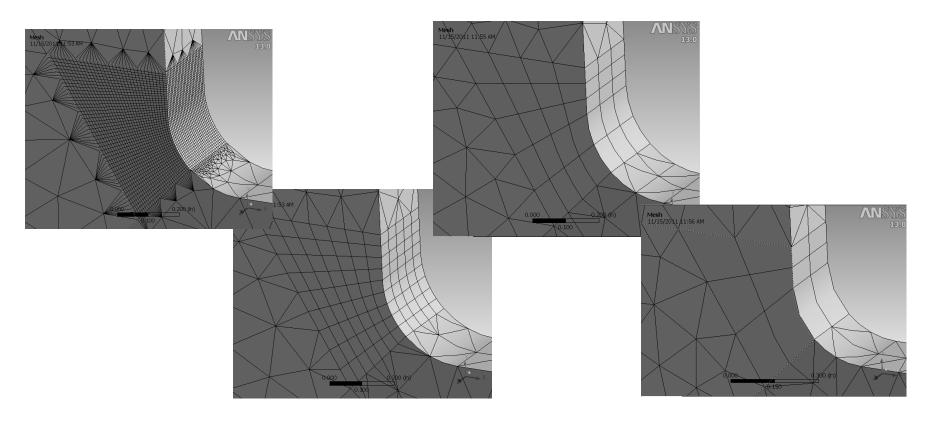




Case Study B

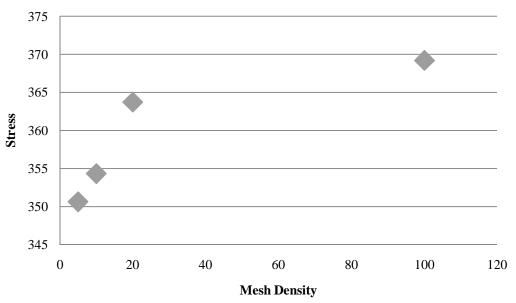


- Stress along path
 - Varying Mesh densities





- Peak Stress
 - Varying Mesh densities
 - WB 's adaptive mesh refinement automates this task refining only regions of interest (thanks, paul)

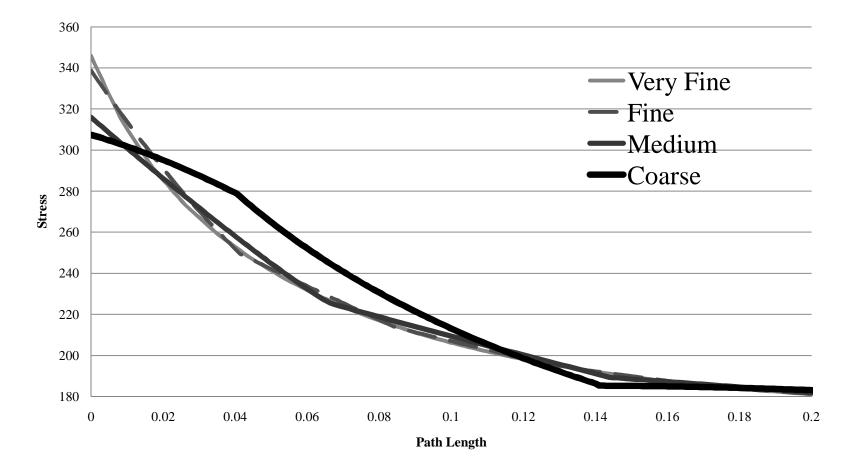


Mesh Convergence

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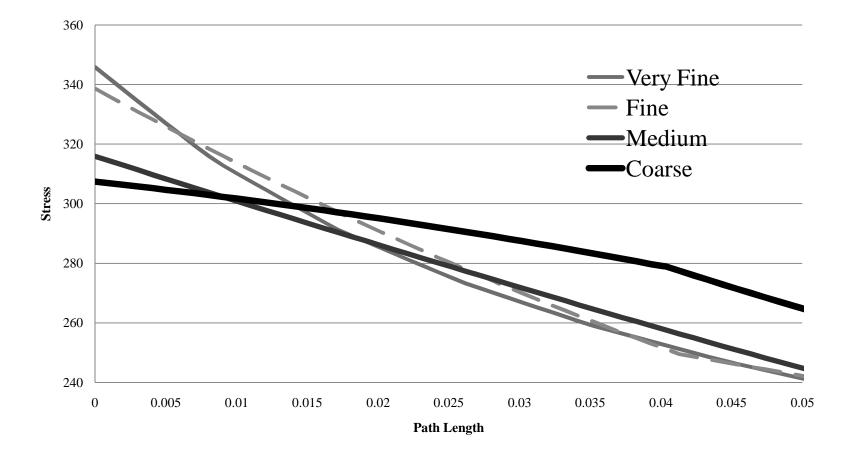


• Stress along path



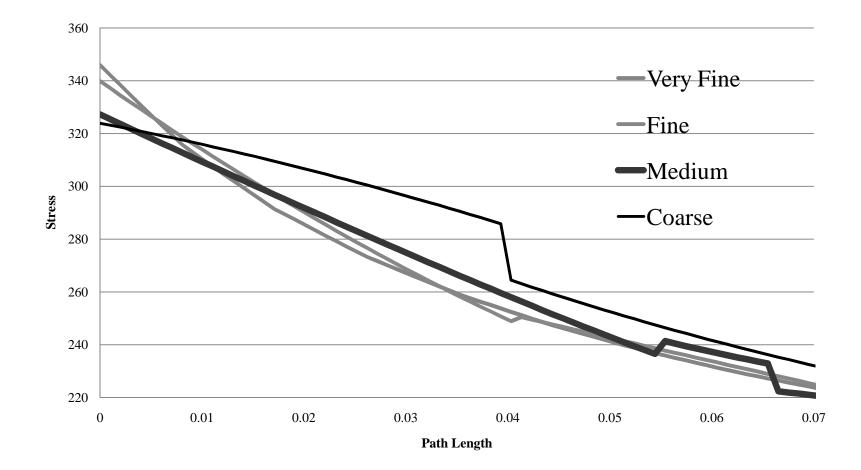


• Stress along path: zoom



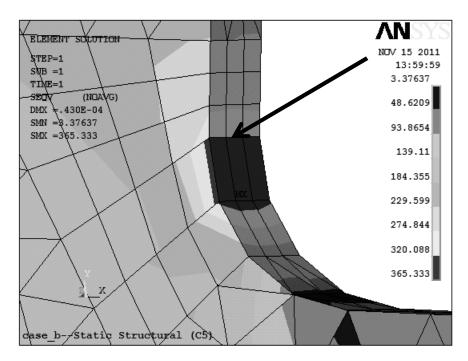


• Stress along path: Unaveraged Results





- Case Study B Conclusion:
 - Discontinuity of stress element-to-element
 relates to degree of mesh discretization error



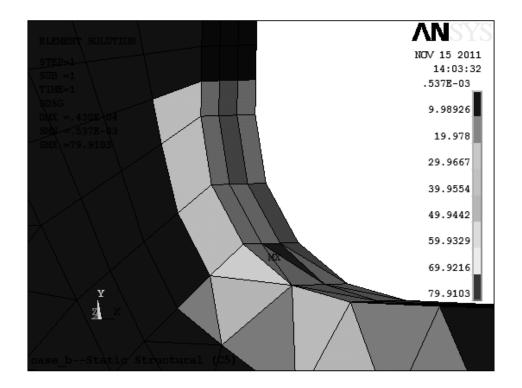
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• Discontinuity at element boundaries is key

 $\{\Delta \sigma_n^i\} = \{\sigma_n^a\} - \{\sigma_n^i\}$ Difference at boundary

85.



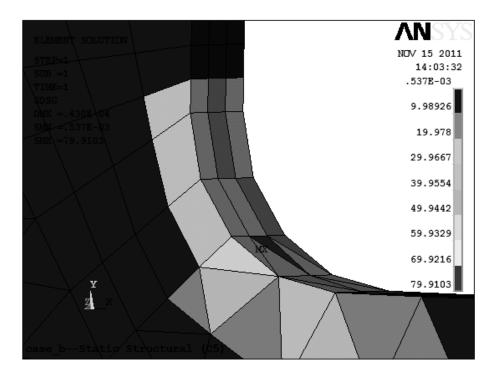


• Discontinuity at element boundaries is key

$$e_{i} = \frac{1}{2} \int_{Vol} \left\{ \Delta \sigma \right\}^{T} \left[D \right]^{-1} \left\{ \Delta \sigma \right\} d(Vol)$$

115-

- Energy difference per element
- Considers volume/stiffness





• Discontinuity at element boundaries is key

$$\mathbf{e} = \sum_{i=1}^{N_{t}} \mathbf{e}_{i}$$

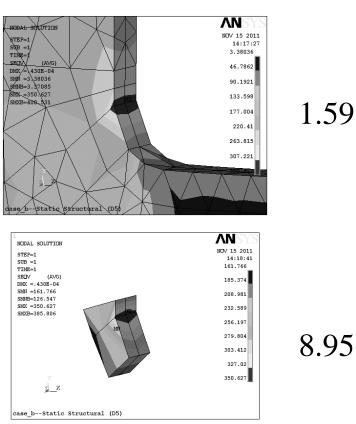
$$\mathbf{E} = 100 \left(\frac{\mathbf{e}}{\mathbf{U} + \mathbf{e}}\right)^{\frac{1}{2}}$$

- Sum it over the model (selected region)
- Normalize it to the whole model energy (includes load magnitude)

Yields a single number! (PRERR, or Percentage error in the energy norm)



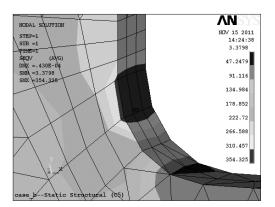
• Percentage error in the energy norm (PRERR)



Coarse

1.59

Medium



ANS NODAL SOLUTION NOV 15 2011 STEP=1 14:26:31 SUB =1 172.69 TIME=1 SEQV (AVG) DMX = .123E-04 (AVG) 195.394 SMN =172.69 218.098 SMX =354.325 240.803 263.507 286.212 308.916 331.62 354.325 z x case_b--Static Structural (C5)

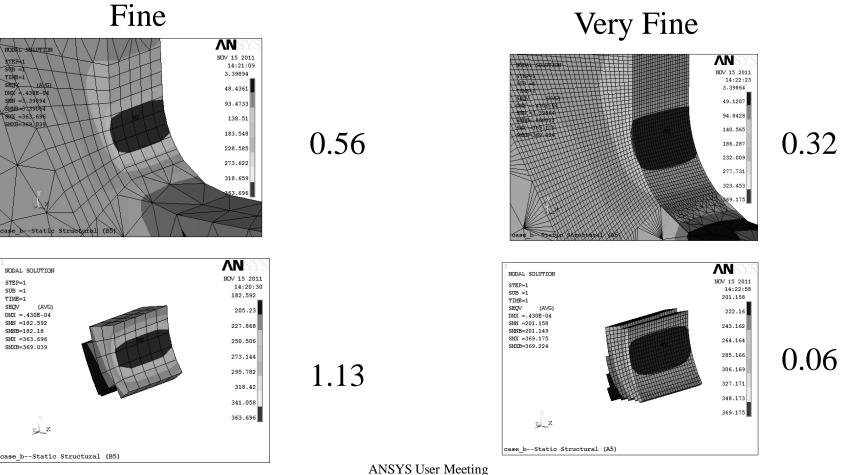
0.797

4.0

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• Percentage error in the energy norm (PRERR)





- SMXB
 - Checks all nodes (doesn't necessarily correspond to the MX location!)
 - Only mentioned once in Help Manual!
 - Training Classes refer to it as a "confidence band"...

